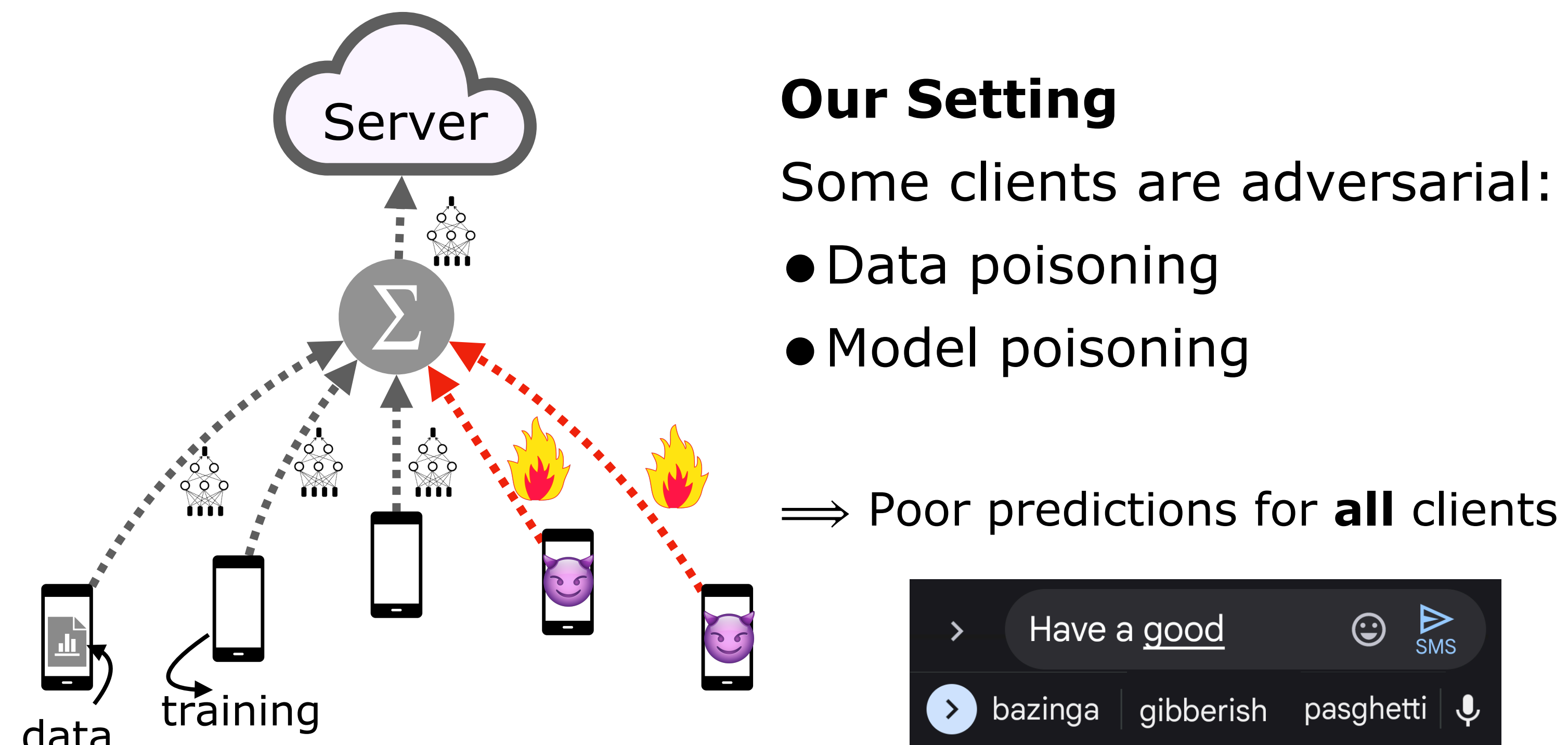




## Robust federated learning



**Objective**  $\min_w \sum_{i \in \mathcal{D}} F_i(w)$

Loss on client  $i$

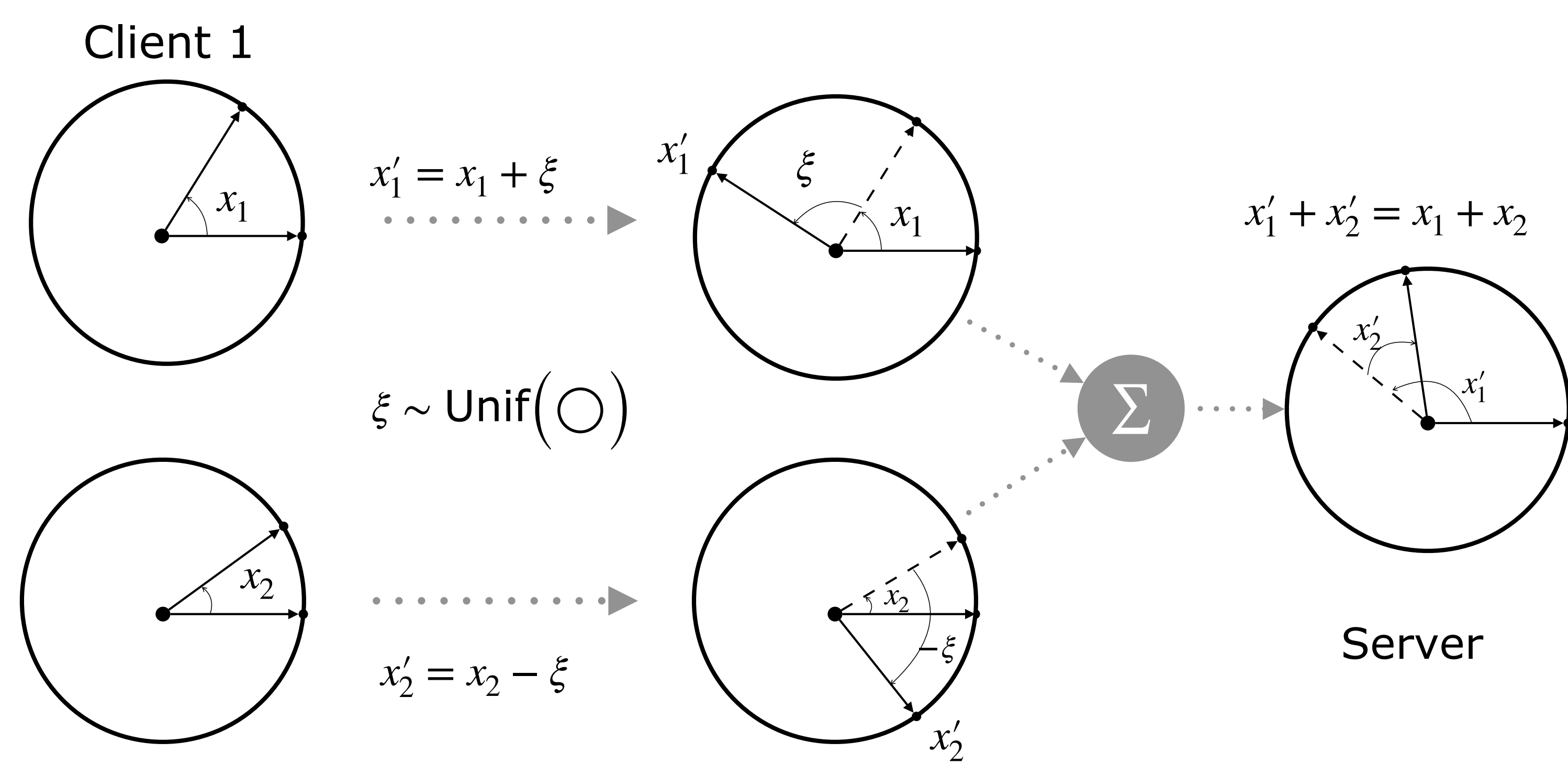
Set of "inlier" clients

## Goals of the work

A robust aggregation approach that is

1. Communication-efficient
2. Implementable via **secure summation**

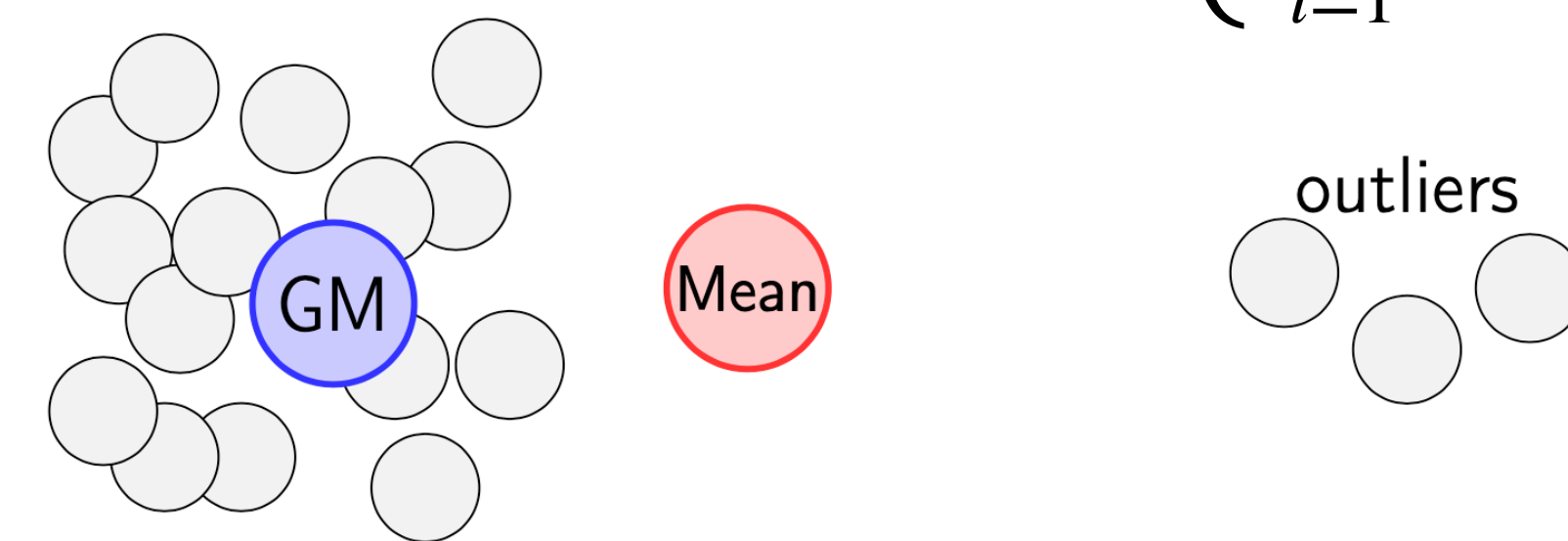
Server only sees  $x'_1, x'_2 \sim \text{Unif}(\bigcirc)$  but calculates the correct sum  $x_1 + x_2 = x'_1 + x'_2$



[Bonawitz et al. CCS (2017), Bell et al. CCS (2020)]

## RFA: Geometric Median Aggregation

$$GM(w_1, \dots, w_m) = \arg \min_z \left\{ \sum_{i=1}^m \|z - w_i\|_2 \right\}$$

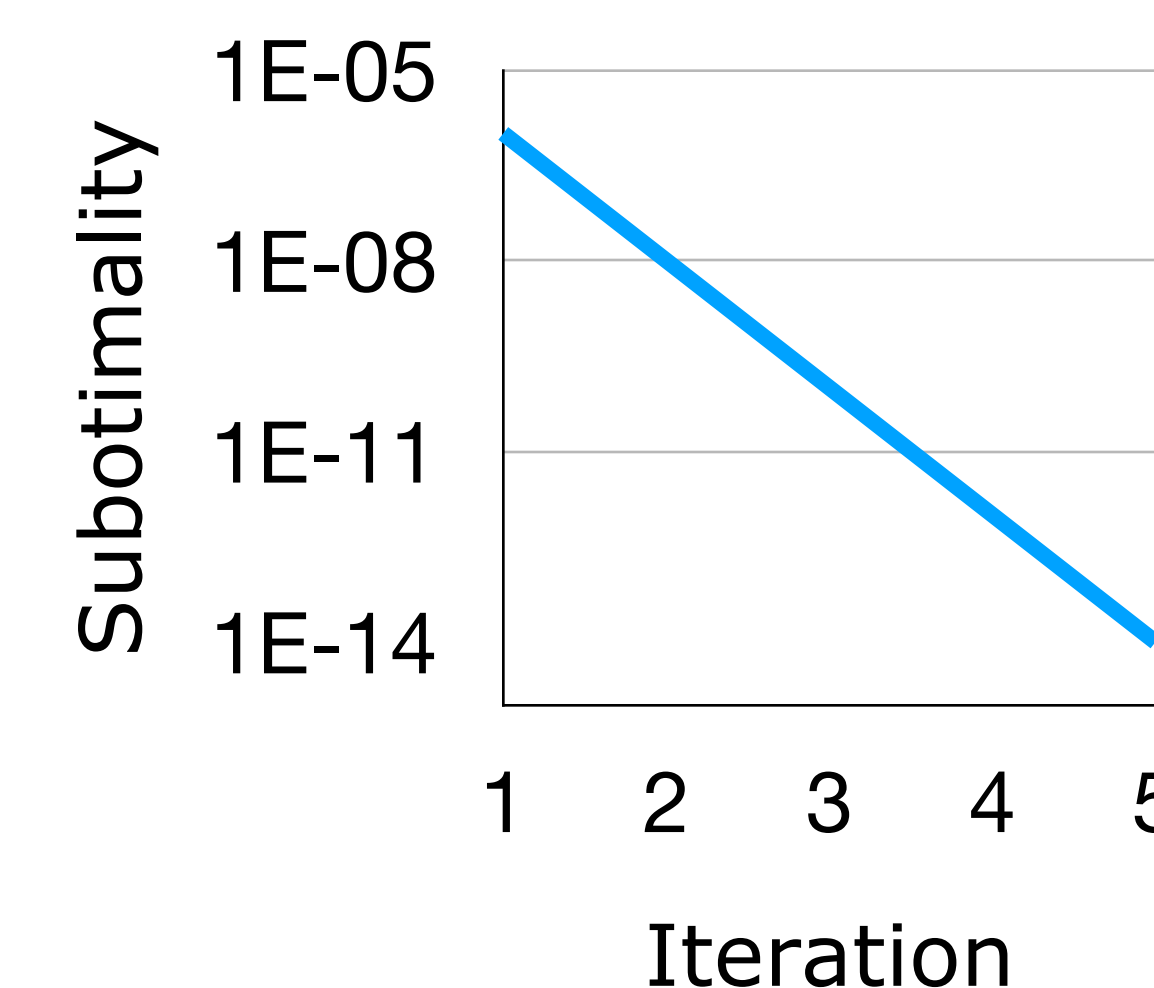


**Robustness:**  
Breakdown point = 1/2

**Weiszfeld's Algorithm:**

$$\beta_{i,t} = 1 / \max\{\|z_t - w_i\|_2, \nu\}$$

$$z_{t+1} = \frac{\sum_i \beta_{i,t} w_i}{\sum_i \beta_{i,t}}$$



## Theory (Least Squares)

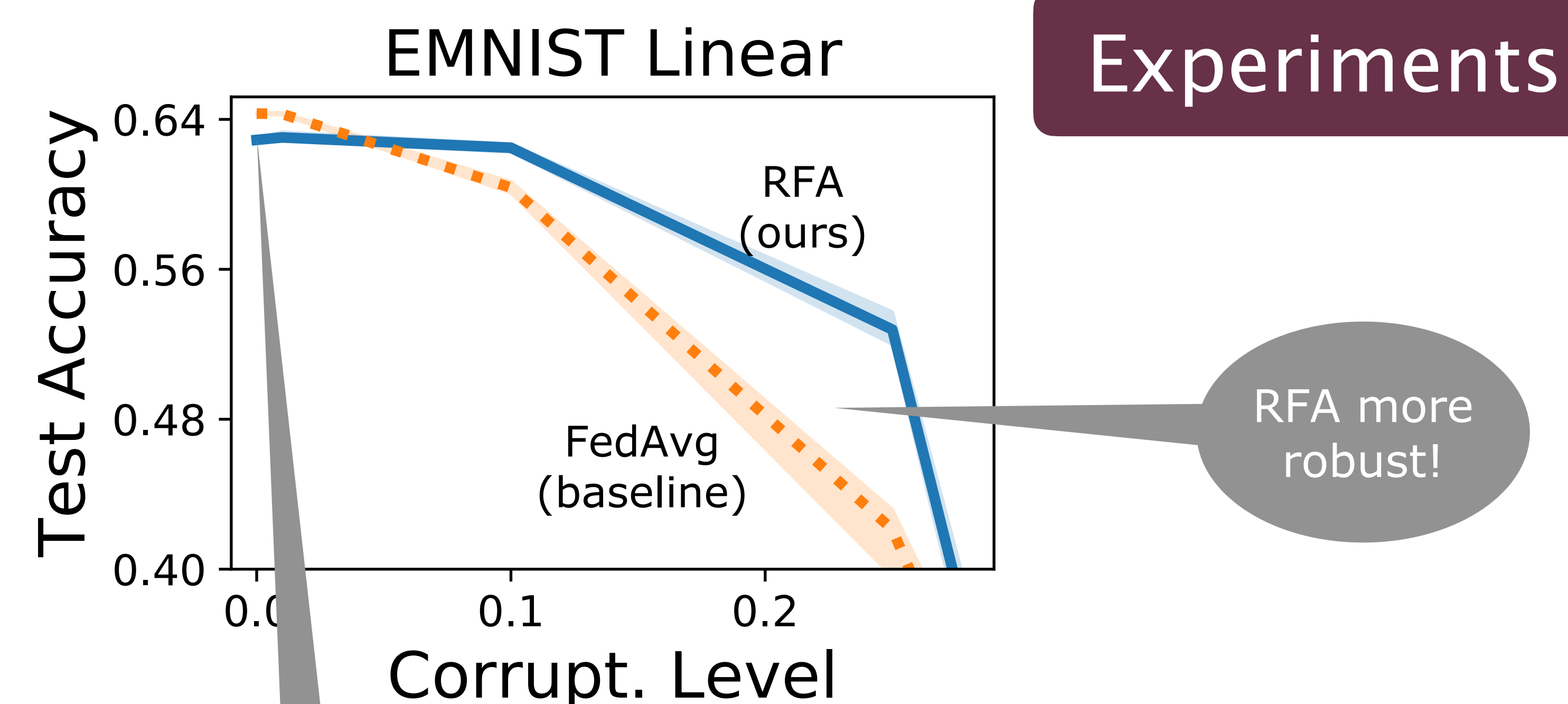
Suppose  $Y_i = X_i^T w_i^* + \xi_i$  where  $\xi_i \sim \mathcal{N}(0, \sigma^2)$

**Theorem:** Assume that  $F(w)$  is strongly convex,  $\|X_i\| \leq 1$  and # local steps  $\propto 2^t$ . Let  $\mathcal{E}$  denote the event that  $\geq 1/2 + c/2$  non-corrupted devices are chosen (out of the  $1/2 + c$  available) in each round.

Then, RFA with  $\epsilon$ -approximate GM satisfies

$$\mathbb{E}[\|w_t - w^*\|^2 | \mathcal{E}] \lesssim \frac{\|w_0 - w^*\|^2}{2^t} + \frac{1}{c^2} \left( d\sigma^2 \frac{t}{2^t} + \frac{\epsilon^2}{m^2} + \Omega_X^2 \Omega_Y^2 \right)$$

Optimization error  
Statistical error  
GM Approx. Error  
**Heterogeneity Error**



**Unavoidable due to lower bounds of robust mean estimation**  
[Chen, Gao, Ren. Annals of Stat. (2018)]

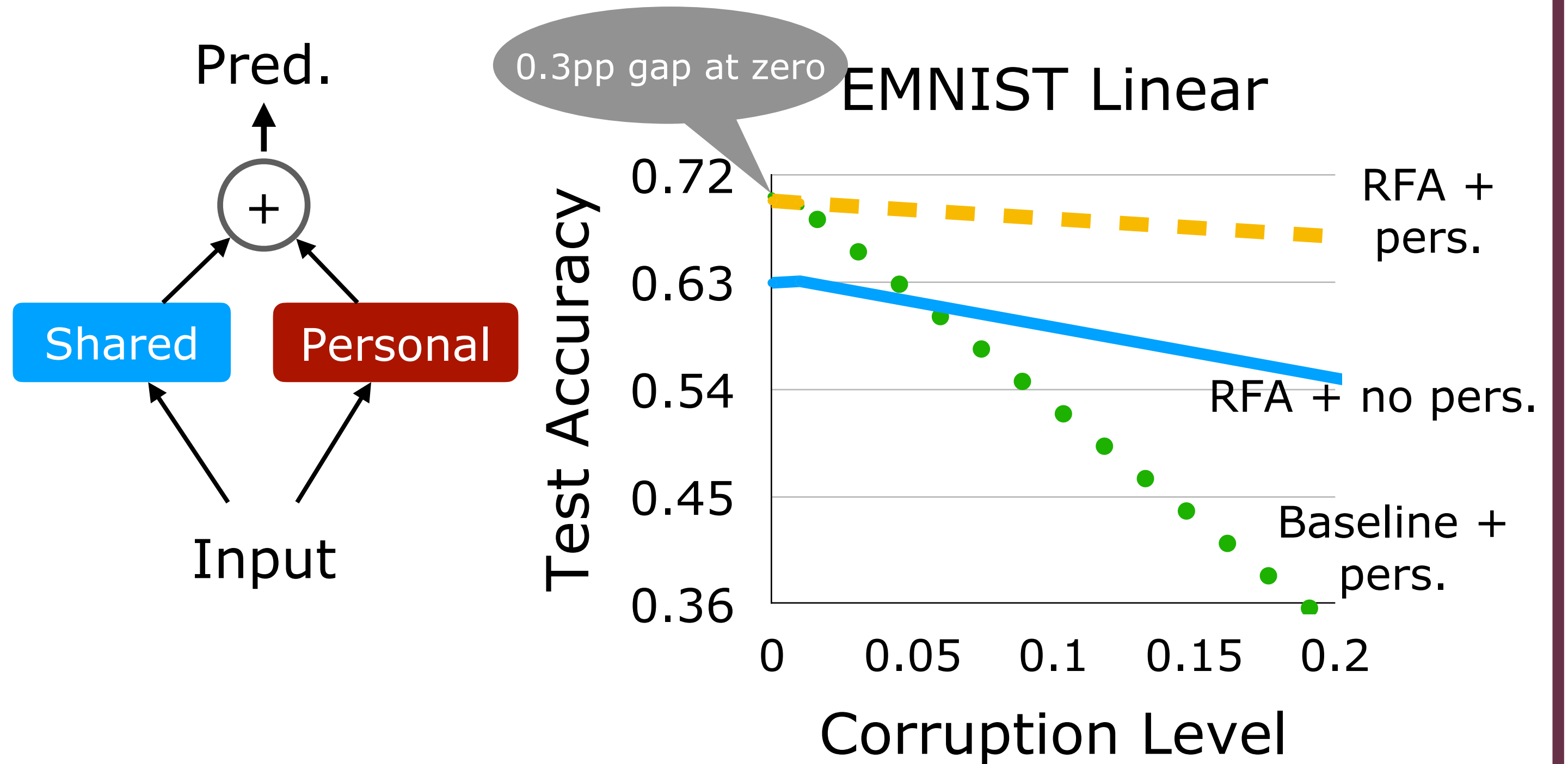
## Experiments

## Handling Heterogeneity

**Personalize parts of the model**

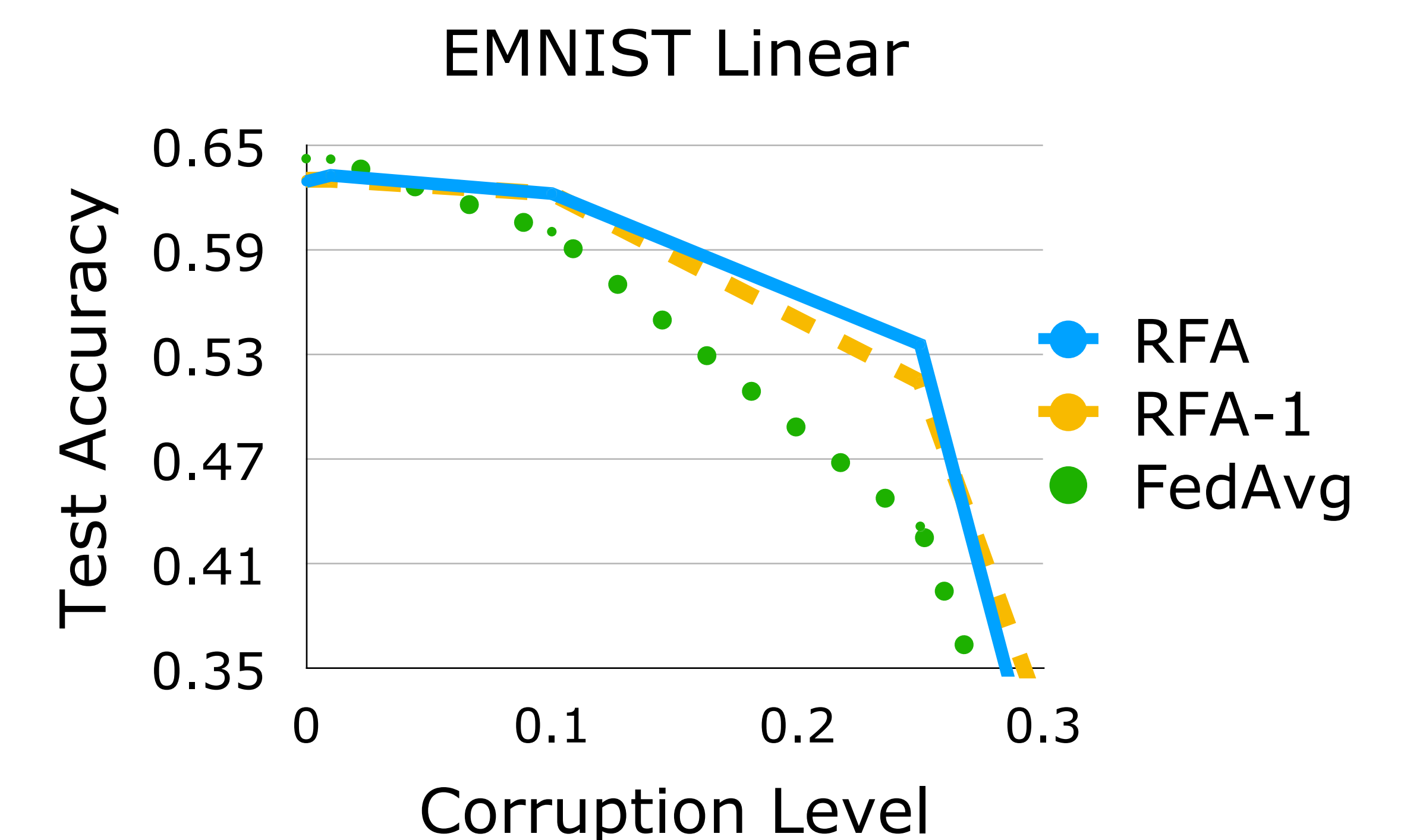
$$\min_{u, v_1, \dots, v_n} \sum_{i \in \mathcal{D}} F_i(u, v_i)$$

$u$ : shared parameters  
 $v_i$ : personal parameters



## Improving the Communication Cost

**Single Weiszfeld iteration is also robust!**



**Software for the geometric median**

Install: `pip install geom-median`

Documentation: [github.com/krishnap25/geom\\_median](https://github.com/krishnap25/geom_median)

krishnap25  
KrishnaPillutla  
[krishnap25.github.io](https://krishnap25.github.io)

**Code**

